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Strong enhancement in thermal conductivity of ethylene glycol-based nanofluids by amorphous and crystalline Al_2O_3 nanoparticles

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In the present work, the temperature and concentration dependence of thermal conductivity (TC) enhancement in ethylene glycol (EG)-based amorphous and crystalline Al_2O_3 nanofluids have been investigated at temperatures ranging from 0 to 100 °C. In our prior study, nanometer-sized particles of amorphous-, γ -, and α - Al_2O_3 were prepared via a simple sol-gel process with annealing at different temperatures and characterized by various techniques. Building upon the earlier study, we probe here the crystallinity, microstructure, and morphology of the obtained α - Al_2O_3 nanoparticles (NPs) by using X-ray powder diffraction with Rietveld full-profile refinement, scanning electron microscopy, and high-resolution transmission electron microscopy, respectively. In this study, we achieved a 74% enhancement in TC at higher temperature (100 °C) of base fluid EG by incorporating 1.0 vol. % of amorphous- Al_2O_3 , whereas 52% and 37% enhancement is accomplished by adding γ - and α - Al_2O_3 NPs, respectively. The amorphous phase of NPs appears to have good TC enhancement in nanofluids as compared to crystalline Al_2O_3 . In a nutshell, these results are demonstrating the potential consequences of Al_2O_3 NPs for applications of next-generation efficient energy transfer in nanofluids. © 2014 AIP Publishing LLC. [<http://dx.doi.org/10.1063/1.4893026>]

To enhance the transport and thermal properties of conventional heat transfer fluids (e.g., water, ethylene glycol (EG), propylene glycol, and engine oil) through nanoparticles additives is an emerging research area in heat transfer science.^{1–9,19} Such increment in the heat transport characteristics of base fluids suggests the crucial benefits which give credence to liquid coolants for moving heat away from electronic, optical, machinery, or nuclear reactor systems.^{5–7,9} Various nanoparticles (NPs) of metals and metal oxides have been added to EG for enhancing the thermal conductivity (TC) of base fluid and are potentially used in heat transfer system.^{2,5–9,19,21,23–25} The nanofluids based on EG reveal a higher TC having nonlinear relationship with temperature.^{23,29} A very recent report to examine the effects of nanoparticle size and temperature has been published focusing on the TC enhancement of water-based Al_2O_3 nanofluids.¹⁰ Owing to the general availability and unique characteristics, such as good structural, chemical and thermal stability at elevated temperatures, high electrical resistivity, low gate leakage, and excellent behavior in optics and electronics, Al_2O_3 in both amorphous and polymorphs (material with similar composition but different crystal structure) forms are registered among the technologically most crucial ceramic materials.^{11–17,27,28}

In this Letter, we evaluated the effects of ordered/disordered structures of Al_2O_3 NPs, volume fraction, and temperatures on the TC enhancement in EG nanofluid for different volume concentrations. As described in a previous work, three different structures of NPs, i.e., amorphous and crystalline γ -, and α - Al_2O_3 , were synthesized by sol-gel method. We performed here the Rietveld full-profile refinement of X-ray diffraction (XRD) pattern and detailed high-resolution

transmission electron microscopy (HRTEM) study of the α - Al_2O_3 NPs. All three kinds of amorphous and crystalline structures of Al_2O_3 NPs were dispersed in EG-base fluid with different particle loadings to prepare Al_2O_3 /EG nanofluids and determine the enhancement in TC experimentally in a temperature range from 0 to 100 °C.

Al_2O_3 NPs were synthesized via sol-gel method with annealing at three different temperatures. First, a 4 ml saturated aqueous solution of aluminium nitrate nonahydrate ($\text{Al}(\text{NO}_3)_3 \cdot 9\text{H}_2\text{O}$) was prepared at room temperature. Then, the saturated solution was heated at 100 °C for 30 min to form the gel and used as the precursor. Finally, the precursor was annealed to obtain Al_2O_3 NPs at 400, 800, and 1000 °C for 2 h inside the muffle furnace. As previously reported, the obtained Al_2O_3 NPs exhibit amorphous (a-), γ -, and α -crystalline structure of the material. For convenience, the three annealed samples were denoted as a- Al_2O_3 , γ - Al_2O_3 , and α - Al_2O_3 , respectively.

The crystal structure information of the synthesized α - Al_2O_3 NPs was determined by XRD (Bruker AXS D8 Advance X-ray diffractometer) using the $\text{Cu-K}\alpha$ ($\lambda = 1.54059 \text{ \AA}$) monochromatic radiation, in the 2θ range between 20° and 79.8°. Structural refinement for refining the crystalline structure of the α -phase in the sample was carried out by the Rietveld method using the program FULLPROF. The morphological identification and size were examined using scanning electron microscope (SEM, Zeiss EVO MA-10) with an acceleration voltage of 10 kV. The high-resolution micrographs in real and reciprocal space were acquired with a HR-TEM (FEI Tecnai G2 F30 STWIN) operated at 300 kV accelerating voltage. Al_2O_3 nanofluids were prepared by dispersing the synthesized Al_2O_3 NPs in EG at three volume percentage of 0.25%, 0.50%, and 1.0%. A hot disc thermal constant analyser

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(model TPS-500) was employed in this study to measure the TC of the corresponding nanofluids within the temperature range of 0–100 °C.

We present the crystallographic structural characteristics and electron microscopy of the synthesized α -Al₂O₃ NPs in Figures 1(a)–1(f). The XRD patterns and morphological details of all three phases (α -, γ -, and α -Al₂O₃) have been discussed in our earlier report.¹¹ However, the α -phase of Al₂O₃ which is well crystalline has been dealt again in the present context in regard to its Rietveld refinement. The Rietveld-refined XRD pattern for the α -phase structure of Al₂O₃ with the observed (red dots), calculated (black solid line), and difference (observed-calculated, blue solid line) spectra is shown in Figure 1(a), resulted in a goodness-of-fit (χ^2) value of 1.19. The XRD pattern exhibited the α -Al₂O₃ NPs crystallized in a rhombohedral structure (space group $R\bar{3}c$, standard JCPDS No. 46-1212) with lattice parameters $a = b = 4.758$ Å and $c = 12.99$ Å. Rietveld-refinement of XRD patterns was performed using the reported parameters of system α -Al₂O₃.^{11,13} The lattice parameters and atomic positions generated by further refinement are listed in Table I. Moreover, all diffraction peaks observed in XRD pattern were sharp and intense suggesting good crystallinity and high purity of the synthesized α -Al₂O₃ NPs. Figures 1(b) and 1(c) represent an enlarged view of the prominent peak intensity identified in XRD pattern for (104) and (113) atomic planes, respectively. The corresponding insets elucidate the fine structure arrangement at atomic-level with lattice spacing of 0.253 nm and 0.208 nm, indicating that NPs of α -Al₂O₃ are defect free. The ball-and-stick representative unit cell of α -Al₂O₃ depicted in Figure 1(d) has a hexagonal crystal structure illustrating their atomic stacking layers consists of alternating aluminium (Al) and oxygen (O) planes, whose stacking sequence is ..-O-Al-Al-O-Al-Al-O-Al-Al-.. in $\langle 0001 \rangle$ direction. In this model, O atoms are drawn

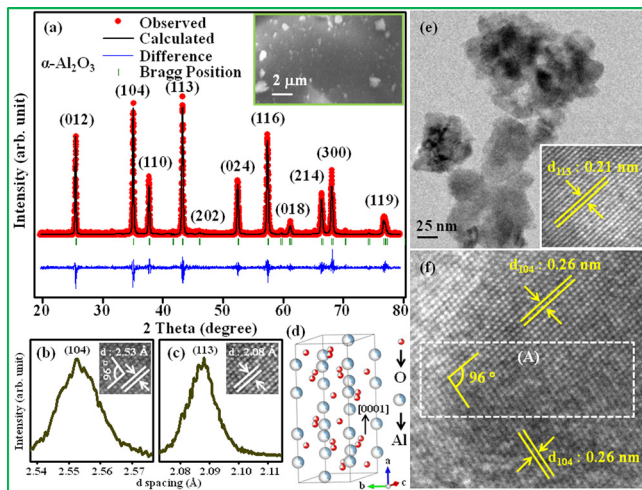


FIG. 1. (a) Rietveld-refined XRD pattern of nano- α -Al₂O₃ synthesized by annealing at 1000 °C, (b) and (c) an enlarged view of prominent peak intensity observed in XRD pattern, (d) schematic hexagonal unit cell of α -Al₂O₃, color code: O, red (small balls) and Al, light blue (large balls), (e) bright-field TEM image, and (f) high-resolution TEM micrograph; zone A (as delineated by white dotted rectangle) indicates the overlapping of lattice planes. Insets: (a) provides spherical-like morphology obtained using SEM, (b) and (c) show HRTEM images to the corresponding (hkl) planes, and (e) elucidates the fine structure arrangement at atomic-level of α -Al₂O₃ nanoparticle.

TABLE I. Rietveld-refined lattice parameters and atomic positions for the α -phase structure of Al₂O₃.

Lattice parameters Space group, $R\bar{3}c$	Profile parameters			
	Function	Pseudo-voigt		
(No. 167)		U = -0.04677		
$a = b = 4.76793$ Å	FWHM parameters	V = 0.11631		
$c = 13.01579$ Å		W = 0.00974		
	Atomic positions			
Atom label	Wyckoff position	x	z	$Occ.$
O	18e	0.3089	0.2500	0.674
Al	12c	0.0000	0.3521	0.352
Reliability factors	R_p : 18.1% R_{wp} : 28.0% R_{exp} : 25.62% $\chi^2 = 1.19$			

smaller and Al atoms are large.¹² In order to explain the crystal structure of α -Al₂O₃, hexagonal unit cell is often more convenient containing 30 atoms (Al = 12 atoms, and O = 18 atoms).^{14,17} The surface morphology of Al₂O₃ NPs is displayed in inset of Figure 1(a), recorded by SEM, illustrating the particles of Al₂O₃ have spherical-like structure and size range from 300 to 500 (± 80) nm. Further insight into the morphology, size, and conformation of NPs has been evaluated by HR-TEM analyses. The subsequent TEM studies elucidate that Al₂O₃ NPs are in dimension of 15–45 nm, as shown in Figure 1(e). Inset in Figure 1(e) provides the high-resolution TEM micrograph which demonstrates clear regular interlattice plane distance of 0.21 nm, consistent with the (113) plane of α -Al₂O₃ crystal, indicating that the NPs of α -Al₂O₃ are perfect and in good crystalline nature. The lattice-resolved HRTEM image elucidates in Figure 1(f) revealing an interlattice plane distance of 0.26 nm, corresponds to (104) plane of α -Al₂O₃, which is almost perpendicular ($\sim 96^\circ$) to each other (denoted by white dotted rectangle area; zone A), further authenticates the high-crystalline nature of α -Al₂O₃ NPs.

We compared the TC of EG-based α -, γ -, and α -Al₂O₃ nanofluids over a broad range of temperature (from 0 to 100 °C) for the particle addition of 0.25, 0.50, and 1.0 vol. %. Three volume concentrations were employed to study the effect of NPs concentration on the TC of base fluid. Figures 2(a), 2(b), and 2(c) represent the temperature-dependent %TC enhancement as a function of NPs additive loading of α -Al₂O₃/EG, γ -Al₂O₃/EG, and α -Al₂O₃/EG nanofluids, respectively. The %TC enhancement can be expressed as follows:

$$\%TC \text{ enhancement} = \left[\frac{K_{nf} - K_{bf}}{K_{bf}} \right] \times 100, \quad (1)$$

where K_{nf} and K_{bf} represents the thermal conductivity of nanofluid and base-fluid, respectively.

Moreover, to predict and explain the TC enhancement in nanofluids, numerous theoretical studies have been focused and debated extensively over the past decade.^{3,10,18–23} Several participating factors include Brownian motion of NPs, internanoparticle potential, radiative heat transfer, particle aggregation, and dynamic interactions have been attempted to account the anomalous enhancement in TC of nanofluids combined with the effects of NPs size and shape, volume concentration of NPs, and temperature.^{2,6,10,19,21–26}

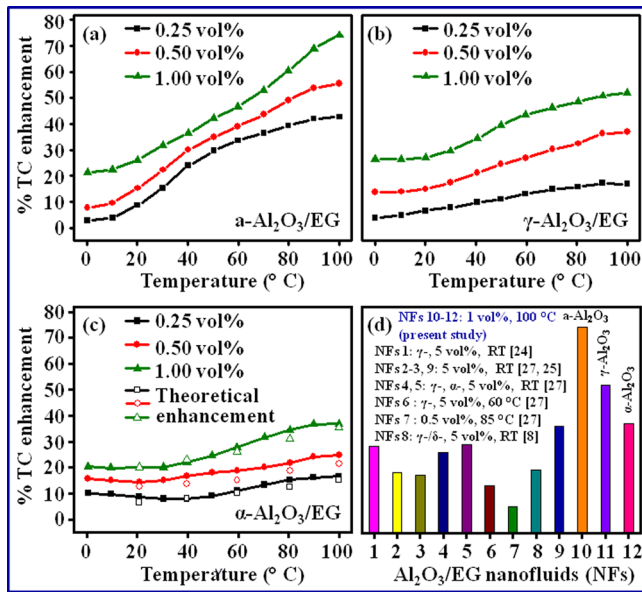


FIG. 2. Temperature dependence of %TC enhancement (TCE) of (a) amorphous-Al₂O₃/EG, (b) γ-Al₂O₃/EG, and (c) α-Al₂O₃/EG nanofluids at NP additive loadings of 0.25, 0.50, and 1.00 vol.%. Color code: black, red, and green (square, circle, and up-triangle in shape) solid (in (a), (b), (c)) and open (in (c)) contours represent experimental and theoretical %TC enhancement, respectively. (d) Histogram illustrating a comparative study of some of the best TCE recorded for different polymorphs Al₂O₃/EG nanofluids in previous literature and in the present study; RT indicates the room temperature.

In addition to describe the enhancement in TC of EG fluid with volume fraction/particle loadings of NPs, the model of Prasher *et al.* for the TC enhancement ratio of nanofluid is given as follows:^{5,6,21}

$$\frac{K_{nf}}{K_{bf}} = (1 + AR_e^m P_r^{0.333} \phi) \left[\frac{(1 + 2\alpha) + 2\phi(1 - \alpha)}{(1 + 2\alpha) - \phi(1 - \alpha)} \right], \quad (2)$$

where ϕ is the particle volume fraction, $\alpha = 2R_b K_{bf} / d_{NP}$, and R_b is the interfacial resistance. P_r is Prandtl number and d_{NP} is diameter of nanoparticle. The Reynolds number R_e can be written as

$$R_e = \frac{1}{\nu} \sqrt{\frac{18k_B T}{\pi \rho_N d_{NP}}}, \quad (3)$$

where ν is the kinematic viscosity, ρ_N is density of the liquid, k_B is Boltzmann constant, and T is temperature in Kelvin scale.

Figure 2(c) provides the order of magnitude calculations for %TC enhancement based on the above model in α-Al₂O₃/EG nanofluid at different particle loadings and temperatures along with the experimental observations. This model includes the effect of particle diameter on TC enhancement of nanofluid. Numerical values of all required parameters are obtained as suggested by the above mentioned model. Here, we have taken $R_b = 9 \times 10^{-8} \text{ K m}^2 \text{ W}^{-1}$, average particle diameter $d_{NP} = 70 \text{ nm}$, $P_r = 10$, and density of Al₂O₃ = 3.95 g/cm³. $A = 40000$ and $m = 2.9$ are beta fit parameters. The calculated %TC values for vol.%- and temperature-dependent seemed to be in good agreement with our experimental investigations. We have measured the TC

TABLE II. Temperature-dependent % thermal conductivity enhancement (TCE) of a-, γ-, and α-Al₂O₃/EG nanofluids for different volume concentrations.

Nanofluids	vol. %	%TCE at different temperatures		
		30 °C	80 °C	100 °C
a-Al ₂ O ₃ /EG	0.25	15.28	39.32	42.70
	0.50	22.27	49.14	55.54
	1.00	31.69	60.42	74.15
γ-Al ₂ O ₃ /EG	0.25	7.70	15.67	16.77
	0.50	17.33	32.44	36.90
	1.00	29.58	48.66	52.03
α-Al ₂ O ₃ /EG	0.25	7.99	15.23	16.58
	0.50	15.14	21.67	24.73
	1.00	20.13	34.48	36.93

of pure a-, γ-, and α-Al₂O₃ powder at room temperature and it is 0.495, 0.459, and 0.377 W/mK, respectively. This difference in TC may be an important reason for difference in TC enhancement in different polymorphs of Al₂O₃.

As expected, the enhancement in TC of Al₂O₃/EG nanofluids is achieved with increasing volume concentrations of NPs and temperatures. We achieve the higher enhancement in TC of EG-based Al₂O₃ nanofluids as displayed in Figure 2(d), histogram demonstrating a comparative study of some of the best TC enhancements recorded for different parameters of Al₂O₃/EG nanofluids. The temperature dependence %TC enhancement at different volume concentrations of a-, γ-, and α-Al₂O₃/EG nanofluids is presented in Table II. The TC enhancement for similar NPs loadings with increasing temperature is more pronounced for a-Al₂O₃/EG nanofluids than for γ- and α-Al₂O₃/EG nanofluids by more than a factor of 1.5 and 2, respectively, which is higher than any of the results reported previously for Al₂O₃/EG nanofluids (Figure 2(d)). The different trends in TC enhancements are probably due to the differences in size of particles, as the particle size decreases, the surface-to-volume ratio of particles increases, can lead to enhance the TC of nanofluids. In our earlier study, the formation of bigger grain like particles is observed with increasing the annealing temperature.¹¹ Although the reason for the observed monotonic trend in the enhancement of TC of nanofluid system can be accounted by the dependence of different crystal structure of NPs or the influence of interfacial between liquid-phase and solid-material, collisions between the base fluid molecule and interfacial thermal resistance may be considered.^{2,6,26} Since nano-amorphous particle is more open structure than nano-crystalline material, in which individually atoms are randomly distributed may form long-range thermal transfer channels, it is clear that particles with different crystallinity influence heat transfer differently, as schematically depicted in Figure 3. The long-range order in nano-crystalline may resist to the liquid-particle interface and resulted in the lower enhanced TC of the crystalline γ- and α-Al₂O₃/EG nanofluids. Moreover, the amorphous structure of Al₂O₃ has random distribution of Al³⁺ and vacancies over tetrahedral (AlO₄), polyhedral (AlO₅), and octahedral (AlO₆) sites with the prominent tetrahedral and octahedral units; whereas the crystal structure of γ-Al₂O₃ is composed of a mixture of tetrahedral and

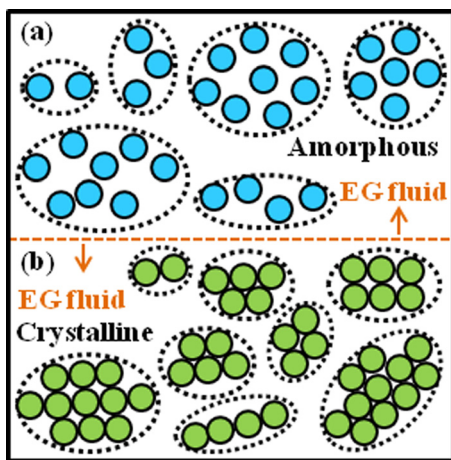


FIG. 3. Schematic representation of the interfacing for the (a) amorphous and (b) crystalline structures of NPs in a base fluid; the blue balls in upper segment indicate the amorphous structure and the green balls in lower segment indicate the crystalline structure of NPs.

octahedral with corner sharing oxygen atoms, and α - Al_2O_3 involved only Al^{3+} in octahedral units.^{12,15,27,28} We infer that the predominant fractions of α - Al_2O_3 NPs may highly interact with the base-fluid and enhance the TC of nanofluids. The lower TC enhancement achieved by the crystalline γ - and α - Al_2O_3 /EG nanofluids can be ascribed due to the presence of short-range interfacing between solid-particle and liquid-phase as compared to the α - Al_2O_3 /EG nanofluids.^{25,30} Based on the results, we conclude that the NPs size, interfacing with liquid, volume fraction of NPs in nanofluids, and temperature affect the TC of Al_2O_3 /EG nanofluids.

In conclusion, we performed the crystallinity determination and morphological identification using Reitveld-refinement XRD analysis and electron microscopy of α - Al_2O_3 NPs. We evaluated the TC enhancement of ethylene glycol-based Al_2O_3 nanofluids, the results corroborate that such nanofluids reveal higher TC than their base fluid and increases with NPs addition and temperatures. We observe, however, that the particle-liquid interfacing is the main reason for the obtained improvement in TC of nanofluids. Such enhancement reveals that Al_2O_3 nanoparticles can be considered as ubiquitous in the advancement for the energy-efficient heat transfer applications.

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